Resolution Number: AC/II(22-23).3.RUS8

S. P. Mandali's

Ramnarain Ruia Autonomous College

Affiliated to Mumbai University



Program: TYBSc

Program Code: (Mathematics) RUSMAT (Credit Based Semester and Grading System for Academic Year 2023-24)

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Graduate Attributes

GA	GA Description-A student completing Bachelor's/Master's Degree in
GA	Mathematics program will be able to:
	Recall and explain acquired scientific knowledge in a comprehensive manner and
GA1	apply the skills acquired in their chosen discipline. Interpret scientific ideas and
	relate its interconnectedness to various fields in science.
	Evaluate scientific ideas critically, analyze problems, explore options for practical
GA2	demonstrations, illustrate work plans and execute them, organize data and draw
	inferences.
	Explore and evaluate digital information and use it for knowledge upgradation.
GA3	Apply relevant information so gathered for analysis and communication using ap-
	propriate digital tools.
GA4	Ask relevant questions, understand scientific relevance, hypothesize a scientific prob-
0711	lem, construct and execute a project plan and analyse results.
	Take complex challenges, work responsibly and independently, as well as in cohesion
GA5	with a team for completion of a task. Communicate effectively, convincingly and in
	an articulate manner.
GA6	Apply scientific information with sensitivity to values of different cultural groups.
0110	Disseminate scientific knowledge effectively for upliftment of the society.
	Follow ethical practices at work place and be unbiased and critical in interpretation
GA7	of scientific data. Understand the environmental issues and explore sustainable
	solutions for it.
	Keep abreast with current scientific developments in the specific discipline and adapt
GA8	to technological advancements for better application of scientific knowledge as a
	lifelong learner



Program Outcomes

	Description-A student completing Bachelor's Degree in Science/Arts pro
РО	gram in the subject of Mathematics will be able to:
	Demonstrate fundamental systematic knowledge of mathematics and its application
PO1	in engineering, science technology and mathematical sciences. It should also enhance
	the subject specific knowledge and help in creating jobs in various sectors.
DO2	Demonstrate educational skills in areas of analysis, algebra, differential equation
PO2	Graph Theory and combinatorics etc.
	Apply knowledge, understanding and skills to identify the difficult / unsolved probable
PO3	lems in mathematics and to collect the required information in possible range
1 05	sources and try to analyse and evaluate these problems using appropriate method
	ologies.
	Fulfil one's learning requirements in mathematics, drawing from a range of con
PO4	temporary research works and their applications in diverse areas of mathematics
	sciences.
PO5	Apply one's disciplinary knowledge and skills in mathematics in newer domains an
	uncharted areas.
PO6	Identify challenging problems in mathematics and obtain well-defined solutions.
PO7	Exhibit subject-specific transferable knowledge in mathematics relevant to job trend
	and employment opportunities.
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CREDIT STRUCTURE BSc

Seme ster	Subje	ct 1	Subject 2	GE/ OE cours e (Acros s discipl ines)	Vocational and Skill Enhanceme nt Course (VSC) & SEC	Ability Enhancement Course/ VEC/IKS	OJT/FP/ CEPCC, RP	Total Credits
1	4		4	4 (2*2)	VSC-2 + SEC -2	AEC- 2 (CSK) + VEC- 2 (Env Sc.) + IKS 2	J.S	22
2	4		4	4 (2*2)	VSC-2	AEC-2 (CSK)+ VEC- 2 (Understandi ng India)	CC-2	22
Tota I	8	A	8	8	8	10	2	44
Exit op	otion: awa					edits and an add		it Core
3	Major 8		Minor 4	2	VSC-2	AEC-2 MIL	FP -2, CC-2	22
4	Major 8		Minor 4	2	SEC-2	AEC-2 MIL	CEP-2, CC-2	22
Total	16		8	4	4	4	8	44

5 DSC DSE Minor 12 4 2 OJT-4 22 Total 24 8 4 2 OJT-4 24 Exit option: award of UG Degree in Major with 132 credits on Continue with Major for Honours/ Research	5 12 4 2 VSC-2 CEP/FP-2 2 6 DSC DSE Minor 12 4 2 Total 24 8 4 2 Exit option: award of UG Degree in Major with 132 credits or Continue							dits and an add		t Core
Total 24 8 4 2 6 44 Exit option: award of UG Degree in Major with 132 credits of Continue with Major for Honours/ Research	Total 24 8 4 2 Exit option: award of UG Degree in Major with 132 credits of Continue with Major for Honours/ Research	5					VSC-2		CEP/FP-2	22
Exit option: award of UG Degree in Major with 132 credits of Continue with Major for Honours/ Research	Exit option: award of UG Degree in Major with 132 credits of Continue with Major for Honours/ Research	6							OJT-4	22
with Major for Honours/ Research	with Major for Honours/ Research	Total	24	8	4		2		5	44
rain Ruiton	All Palis All Pa		Exit o	ption: av					Continue	
						7	XIII.			



Program Outline FYBSc for Mathematics

Course Code	Unit	Topics	Credits	L/Week
		Semester-1 Calculus I		10
	Unit I	Real Number System		
RUSMAT.O101	Unit II	Sequences	3	\bigcirc_3
	Unit III	Limits & Continuity		
		Practicals Based on Unit-1, Unit-2 and Unit-III	(2)	2
	Sen	nester-1 Computations with Sagemath		I
	Unit I	Introduction to Sagemath	1	1
RUSVSCMAT.O101		Practicals in Sagemath	1	2
		Semester-2 Calculus II		I
	Unit I	Continuity of a function on an interval		
RUSMAT.E111	Unit II	Differentiability and its applications	3	3
	Unit III	Series		
		Practicals Based on Unit-1, Unit-2 and Unit-III	1	2
	Se	emester-2 Computations with Scilab		1
	Unit I	Introduction to Scilab	1	1
RUSSECMAT.E111		Practicals in Scilab	1	2
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Program Outline

SYBSc

Semester III

Course Code	Unit	Topics	Credits	L/Week
	<u> </u>	Calculus III		
	Unit I	Riemann Integration		
RUSMAT301	Unit II	Applications of Integration	130	3
	Unit III	Improper Integrals		
		Linear Algebra II	,	
	Unit I	Linear Transformations and Matrices		
RUSMAT 302	Unit II	Determinants	3	3
	Unit III	Inner Product Spaces		
		Discrete Mathematics		
	Unit I	Preliminary Counting		
RUSMAT 303	Unit II	Advanced Counting	3	3
	Unit III	Permutations and Recurrence Relations.		
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Program Outline

SYBSc

Semester IV

Course Code	Unit	Topics	Credits	L/Wee
	I	Calculus of Several Variables		O'
	Unit I	Functions of Several Variables)
RUSMAT401	Unit II	Differentiation	$\stackrel{\circ}{\smile}$ 3	3
	Unit III	Applications		
		Linear Algebra III	<u> </u>	
	Unit I	Quotient Spaces and Orthogonal Linear Transformations		
RUSMAT402	Unit II	Eigenvalues and Eigenvectors	3	3
	Unit III	Diagonalization		
		Ordinary Differential Equations		
RUSMAT403	Unit I Unit II	First order ordinary differential equations Second order ordinary differential equations	3	3
	Unit III	Numerical Methods for Ordinary differential Equations		
Pail.				



Program Outline

TYBSc

${\bf Semester} \,\, {\bf V}$

		Integral Calculus			
Course Code	Unit	Topics	Credits	L/Week	
	I	Multiple Integrals	1		
RUSMAT501	II	Line Integrals	2,5	3	
	III	Surface Integrals			
		Algebra II			
	I	Group Theory			
RUSMAT502	II	Normal Subgroups	2.5	3	
	III	Direct Products of Groups			
		Topology of Metric Spaces	,		
	I	Metric Spaces			
RUSMAT503	II	Closed Sets; Sequences and Completeness	2.5	3	
	III	Continuity			
		Graph Theory (Elective I)			
	I °	Rasics of Graphs			
RUSMATE504I	IF	Trees	2.5	3	
	JI II	Eulerian and Hamiltonian graphs			
Number Theory and its Applications (Elective II)					
	I	Congruences and Factorization			
RUSMATE504II	II	Diophantine Equations and their Solutions	2.5	3	
>	III	Primitive Roots and Cryptography			



$\begin{array}{c} \textbf{Program Outline} \\ \textbf{TYBSc} \end{array}$

Practicals Course Semester V

\mathbf{Course}	Practicals	Credits	$\mathbf{L} \mathbf{W} \mathbf{eek}$
RUSMATP501	Practicals based on RUSMAT501	3	6
	and RUSMAT502	120	
RUSMATP502	Practicals based on RUSMAT503		
	RUSMATE504I or RUSMATE504II	3	6
	RUSMATE 504II		



$\begin{array}{c} \textbf{Program Outline} \\ \textbf{TYBSc} \\ \textbf{Semester VI} \end{array}$

Course Code	Unit	Topics	Credits	L/Week
		Basic Complex Analysis	I.	
	I	Complex Numbers and Functions of a Complex Variable		10
RUSMAT601	II	Holomorphic Functions	2.5	3
	III	Complex Power Series		O
		Algebra III)
	I	Ring Theory	5	
RUSMAT602	II	Factorization	2.5	3
	III	Field Theory	_	
		Metric Topology	I	
	I	Compact Sets		
RUSMAT603	II	Connected Sets	2.5	3
	III	Function Spaces and Fourier Series		
		Graph Theory and Combinatorics (Elective I)	I	
	I	Colorings of a Graph		
RUSMAT604I	II	Planar Graph	2.5	3
	III	Combinatorics	-	
	Nı	imber Theory and its Applications II (Elective II)	I.	
	I	Quadratic Reciprocity		
RUSMATE604II	II	Continued Fractions	2.5	3
	III	Pells Equation, Arithmetic Functions, Special Numbers	_	
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$\begin{array}{c} \textbf{Program Outline} \\ \textbf{TYBSc} \end{array}$

Practicals Course Semester VI

RUSMATP601	Described a land and DUCMATICAL		1
	Practicals based on RUSMAT601	3	6
	and RUSMAT602		
RUSMATP602	Practicals based on RUSMAT603,		
	RUSMATE604I or RUSMATE604II	3	6
Ranna	RUSMATE604II		



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Detailed Syllabus

FYBSc

Semester I

Department Specific Course

Subject-1 Course Code:RUSMAT.O101

Course Title: Calculus I Academic Year: 2023-24

CO	CO Description
CO1	to explain the properties of real numbers.
CO2	to explain the notions of convergent sequences.
CO3	to outline the concepts of limits and continuity.
CO4	to apply the concepts of limits and continuity in the fields of economics, physics and biological sciences.

Unit I: Real Number System (15 Lectures)

Real number system R and order properties of R, Absolute value |.| and its properties.

Bounded sets, statement of l.u.b. axiom, g.l.b. axiom and its consequences, Supremum and infimum, Maximum and minimum, Archimedean property and its applications, density of rationals, Cantors nested interval theorem.

AM-GM inequality, Cauchy-Schwarz inequality, intervals and neighbourhoods, Hausdorff property_

Unit II: Sequences (15 Lectures)

Definition of a sequence and examples, Convergence of sequence, every convergent sequence is



bounded, Limit of a convergent sequence and uniqueness of limit, Divergent sequences. Algebra of convergent sequences, sandwich theorem.

Convergence of standard sequences like

$$\left(\frac{1}{1+na}\right) \ \forall \ a>0, \ \ (b^n), \ \ |b|<1, \ \ \left(c^{1/n}\right) \ \forall \ c>0 \ \mathrm{and} \ \left(n^{1/n}\right),$$

monotone sequences, convergence of monotone bounded sequence theorem and consequences such as convergence of $\left(\left(1+\frac{1}{n}\right)^n\right)$.

Definition of subsequence, subsequence of a convergent sequence is convergent and converges to the same limit. Every sequence in R has a monotonic subsequence. Bolzano-Weierstrass Theorem. Definition of a Cauchy sequence, every convergent sequence is a Cauchy sequence.

Unit III: : Limits and Continuity (15 Lectures)

Brief review: Domain and range of a function, injective function, surjective function, bijective function, composite of two functions (when defined), Inverse of a bijective function.

Graphs of some standard functions such as |x|, e^x , $\log x$, $ax^2 + bx + c$, $\frac{1}{x}$, x^n $(n \ge 3)$, $\sin x$, $\cos x$, $\tan x$, $x \sin \left(\frac{1}{x}\right)$, $x^2 \sin \left(\frac{1}{x}\right)$ over suitable intervals of \mathbb{R}

 $\varepsilon-\delta$ definition of limit of a real valued function of real variable. Evaluation of limit of simple functions using the definition, uniqueness limit if it exists, algebra of limits, limit of composite function, sandwich theorem, left-hand limit $\lim_{x\to a^-} f(x)$, right-hand limit $\lim_{x\to a^+} f(x)$, non existence of limits, $\lim_{x\to -\infty} f(x)$, $\lim_{x\to \infty} f(x)$ and $\lim_{x\to a} f(x) = \pm \infty$.

Continuous functions: Continuity of a real valued function on a set in terms of limits, examples, Continuity of a real valued function at end points of domain, Sequential continuity, Algebra of continuous functions, Discontinuous functions, examples of removable and essential discontinuity.

	Practicals Based on Course : Calculus-1				
Sr. No.	Practicals				
1	Application based examples of Archimedean property, intervals, neighbourhood.				
2	Consequences of l.u.b. axiom, infimum and supremum of sets.				
37	Calculating limits of sequences.				
4	Cauchy sequences, monotone sequences.				
5	Limit of a function and Sandwich theorem.				
6	Continuous and discontinuous functions.				



Reference Books:

- (1) R. R. Goldberg, Methods of Real Analysis, Oxford and IBH, 1964.
- (2) K.G. BINMORE, Mathematical Analysis, Cambridge University Press, 1982.
- (3) R.G. Bartle, D.R. Sherbert, Introduction to Real Analysis, John Wiley & Sons, 1994.
- (4) T. M. Apostol, Calculus Volume I, Wiley & Sons (Asia) Pvt. Ltd, 1991.
- (5) R. Courant, F. John, A Introduction to Calculus and Analysis, Volume I, Springer
- (6) A. Kumar, S. Kumaresan, A Basic Course in Real Analysis, CRC Press, 2014
- (7) J. Stewart, Calculus, Third Edition, Brooks/Cole Publishing Company, 1994.
- (8) S. R. GHORPADE, B. V. LIMAYE, A Course in Calculus and Real Analysis, Springer

15



VSC Course Code: RUSVSCMAT.O101 Course Title:Computations with Sagemath Academic Year: 2023-24

CO	CO Description	
CO1	To define and manipulate functions and symbols in Sagemath	
CO2	Use Sagemath as a calculator	2
CO3	Use of graphics in Sagemath	

Introduction to SageMath

- 1. Sage installation and use in various platforms. Using SageMath as an advanced calculator.
- 2. Defining functions and exploring concept of calculus.
- 3. Finding roots of functions and polynomials.
- 4. Plotting graph of 2D and 3D in SageMath.

	Practical on VSC :Computations with Sagemath				
Sr. No.	Practicals				
1	Defining functions and symbols in Sagemath				
2	Plotting graphs using Sagemath				
3	Manipulations with polynomials using Sagemath				
4	Basic numerical methods using Sagemath				

References:

1. George A. Anastassiou, Razvan A. Mezei (auth.)-Numerical Analysis Using Sage-Springer International Publishing (2015)



Modalities of Assessment

Theory Examination Pattern

(A) Internal Assessment - 30 Marks

Sr. No.	Evaluation Type	Marks
1	Test	20
2	Assignment/Viva/Test/Presentation	10
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Total: 30 Marks

(B) External Examination- 45 Marks

- 1. Duration: These examinations shall be of **two hours duration**.
- 2. Theory Question Pattern

Question	Marks	Questions Based on
Question 1	15	Unit-I
Question 2	15	Unit-II
Question 3	15	Unit-IN

(C) Practical Examination - 50 Marks

Sr. No.	Evaluation Type	Marks		
1	Assignment/Viva/Test/Presentation	20		
2	Practical Examination	30		
Total: 50 Marks				

Overall Examination and Marks Distribution Pattern Semester-I

Course	RUSMAT.O101			se RUSMAT.O101 RUSMATP.O101			Grand Total
No.	Internal	External	Total	Internal	External	Total	
Theory	30	45	75	20	30	50	125



Detailed Syllabus

FYBSc

Semester II

Department Specific Course

Subject-1 Course Code: RUSMAT.E111
Course Title: Calculus-II
Academic Year: 2023-24

СО	CO Description
CO1	to analyze the properties of continuous functions.
CO2	to identify differentiable functions.
CO3	to analyze properties of differentiable functions.
CO4	to test the convergence of series.

Unit I: Continuity of a function on an interval (15 Lectures)

Review of the definition of continuity (at a point and on the domain). Uniform continuity, sequential continuity, examples.

Properties of continuous functions such as the following:

- 1. Intermediate value property
- 2. A continuous function on a closed and bounded interval is bounded and attains its bounds.
- 3. If a continuous function on an interval is injective then it is strictly monotonic and inverse function is continuous and strictly monotonic.
- 4. A continuous function on a closed and bounded interval is uniformly continuous.

Unit IL Differentiability and Applications (15 Lectures)

Differentiation of a real valued function of one variable: Definition of differentiation at a point of an open interval, examples of differentiable and non differentiable functions, differentiable functions are continuous but not conversely, algebra of differentiable functions.



Chain rule, Higher order derivatives, Leibnitz rule, Derivative of inverse functions, Implicit differentiation (only examples).

Rolle's Theorem, Lagrange's and Cauchy's mean value theorems, applications and examples

Taylor's theorem with Lagrange's form of remainder (without proof), Taylor polynomial and applications

Monotone increasing and decreasing function, examples

Definition of local maximum and local minimum, necessary condition, stationary points, second derivative test, examples, concave, convex functions, points of inflection. Applications to curve sketching.

L'Hospital's rule without proof, examples of indeterminate forms.

Unit III: Series (15 Lectures)

Series $\sum_{n=1}^{\infty} a_n$ of real numbers, simple examples of series, Sequence of partial sums of a series, convergence of a series, convergent series, divergent series, Necessary condition: $\sum_{n=1}^{\infty} a_n$ converges $\Rightarrow a_n \to 0$, but converse is not true, algebra of convergent series, Cauchy criterion, divergence of harmonic series, convergence of $\sum_{n=1}^{\infty} \frac{1}{n^p}$ (p > 1), Comparison test, limit comparison test, alternating series, Leibnitz's theorem (alternating series test) and convergence of $\sum_{n=1}^{\infty} \frac{(-1)^n}{n}$, absolute convergence, conditional convergence, absolute convergence implies convergence but not conversely, Ratio test (without proof), Root test (without proof), and examples.

	Practicals Based on Subject-1 Calculus-II
Sr. No.	Practicals
1	Calculating limit of series, Convergence tests.
2	Properties of continuous functions.
3	Differentiability, Higher order derivatives, Leibnitz theorem.
4	Mean value theorems and its applications.
3	Extreme values, increasing and decreasing functions.
6,	Applications of Taylor's theorem and Taylor's polynomials.



Reference Books:

- (1) R. R. Goldberg, Methods of Real Analysis, Oxford and IBH, 1964.
- (2) J. Stewart, Calculus, Third Edition, Brooks/cole Publishing Company, 1994
- (3) T. M. APOSTOL, Calculus Vol I, Wiley & Sons (Asia).
- (4) R. Courant, F. John, A Introduction to Calculus and Analysis, Volume I, Springer.
- (5) A. Kumar, S. Kumaresan, A Basic Course in Real Analysis, CRC Press, 2014
- (6) S. R. GHORPADE, B. V. LIMAYE, A Course in Calculus and Real Analysis, Springer International Ltd, 2006.
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Modalities of Assessment

Theory Examination Pattern

(A) Internal Assessment - 30 Marks

Sr. No.	Evaluation Type	Marks
1	Test	20
2	2 Assignment/Viva/Test/Presentation	
	Total: 30 Marks	• 0

(B) External Examination- 45 Marks

- 1. Duration: These examinations shall be of **two hours duration**.
- 2. Theory Question Pattern

Question	Marks	Questions Based on
Question 1	15	Unit-I
Question 2	15	Unit-II
Question 3	15	Unit-IN

(C) Practical Examination - 50 Marks

Sr. No.	Evaluation Type	Marks
DI. 110.		Warks
1	Assignment/Viva/Test/Presentation	20
2	Practical Examination	30
	Total: 50 Marks	

Overall Examination and Marks Distribution Pattern Semester-II

Course	RUS	SMAT.E1	11	RUS	MATP.E1	Grand Total	
	Internal External		Total	Internal	External	Total	
Theory	30	45	75	20	30	50	125



VSC Course Code: RUSSECMAT.E111 Course Title:Computations with Scilab Academic Year: 2023-24

CO	CO Description	
CO1	To define and manipulate functions and symbols in Scilab	
CO2	Use Scilab as a calculator	
CO3	to learn basic programming in Scilab	

Programming in Scilab

- 1. Basic introduction to SciLab, using SciLab as an advanced calculator.
- 2. Defining vectors and matrices and basic operations.
- 3. Plotting graphs in 2D and 3D in various forms.
- 4. Programming in Scilab

	Practicals Based on Scilab							
Sr. No.	Practicals							
1	Use of Scilab as a calculator							
2	Plotting of various types of graphs using Scilab							
3	Applied linear algebra using Scilab							
4	Basic numerical methods using Scilab							

References:

- 1. SciLab Textbook Companion For Higher Engineering Mathematics, B. S. Grewal.
- 2. SciLab Textbook Companion For Linear Algebra and Its Applications, D. C. Lay.
- 3. SciLab Textbook Companion For Numerical Methods, E. BalguRUSwamy.
- 4. Introduction to SciLab, Sandeep Nagar, Apress.



Course Code: RUSMAT301 Course Title:Calculus III Academic Year: 2023-24

СО	CO Description	
CO1	to identify Riemann Integrable functions.	
CO2	to analyze applications of integration.	20
CO3	to test the convergence of improper integrals.	20

 $\bf Note : \ Review \ of \ lim \ inf \ and \ lim \ sup.$

Unit I: Riemann Integration(15 Lectures)

- 1. Approximation of area, Upper/Lower Riemann sums and properties, Upper/Lower integrals.
- 2. Concept of Riemann integration, criterion for Riemann integrability
- 3. Properties of Riemann integrable functions.
- 4. Basic results on Riemann integration.
- 5. Indefinite integrals and its basic properties.

Unit II: Applications of Integration (15 Lectures)

- 1. Average value of a function, Mean Value Theorem of Integral Calculus
- 2. Area between the two curves.
- 3. Arc length of a curve.
- 4 Surface area of surfaces of revolution
- 5. Volumes of solids of revolution, washer method and shell method.
- 6. Definition of the natural logarithm $\ln x$ as $\int_1^x \frac{1}{t} dt$, x > 0, basic properties.



- 7. Definition of the exponential function $\exp x$ as the inverse of $\ln x$, basic properties.
- 8. Power functions with fixed exponent or with fixed base, basic properties.

Unit III: : Improper Integrals (15 Lectures)

- 1. Definitions of two types of improper integrals, necessary and sufficient conditions for convergence.
- 2. Absolute convergence, comparison and limit comparison test for convergence. Abel's and Dirichlet's tests.
- 3. Gamma and Beta functions and their properties.

	Tutorials Based on Course : RUSMAT301							
Sr. No.	Tutorials							
1	Calculation of upper sum, lower sum and Riemann integral.							
2	Problems on properties of Riemann integral.							
3	Sketching of regions in \mathbb{R}^2 and \mathbb{R}^3 , graph of a function, level sets, conversions from							
3	one coordinate system to another.							
4	Applications to compute average value, area, volumes of solids of revolution, surface							
4	area of surfaces of revolution, moment, center of mass.							
5	Convergence of improper integrals, applications of comparison tests, Abel's and							
3	Dirichlet's tests, and functions.							
6	Problems on Gamma, Beta functions and properties							

Reference Books:

- (1) R. R. GOLDBERG, Methods of Real Analysis, Oxford and IBH, 1964.
- (2) A. Kumar, S. Kumaresan, A Basic Course in Real Analysis, CRC Press, 2014.
- (3) S. R. Ghorpade, B. V. Limaye, A Course in Calculus and Real Analysis, Springer International Ltd., 2000.
- (4) T. M. APOSTOL, Calculus Volume I, Wiley & Sons (Asia) Pvt. Ltd.
- (5) T. M. Apostol, Mathematical Analysis, Second Ed., Narosa, New Delhi, 1974.



- (6) J. Stewart, Calculus, Third Ed., Brooks/Cole Publishing Company, 1994.
- (7) R. COURANT, F. JOHN, Introduction to Calculus and Analysis, Vol I. Reprint of 1st Ed. Springer-Verlag, New York, 1999.
- (8) M. H. Protter, Basic Elements of Real Analysis, Springer-Verlag, New York, 1998.
- (9) G.B. Thomas, R. L. Finney, Calculus and Analytic Geometry, Ninth Ed. (ISE Reprint), Addison-Wesley, Reading Mass, 1998.
- (10) R.G. Bartle, D.R. Sherbert, Introduction to Real Analysis, John Wiley & Sons,

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Course Code: RUSMAT302 Course Title: Linear Algebra II Academic Year: 2023-24

СО	CO Description
CO1	to examine dimensions of vector spaces.
CO2	to explain the concept of determinants.
CO3	to apply the concept of determinants to geometry.
CO4	to identify inner product spaces.
CO5	to outline properties of inner products.

Unit I: Linear Transformations and Matrices (15 Lectures)

- 1. Review of linear transformations, kernel and image of a linear transformation, Rank-Nullity theorem (with proof), linear isomorphisms, inverse of a linear isomorphism, any n-dimensional real vector space is isomorphic to \mathbb{R}^n .
- 2. The matrix units, row operations, elementary matrices and their properties.
- 3. Row Space, column space of $m \times n$ matrix, row rank and column rank of a matrix, equivalence of the row and column rank, Invariance of rank upon elementary row or column operations.
- 4. Equivalence of rank of an $m \times n$ matrix A and rank of the corresponding linear transformation, The dimension of solution space of the system of the linear equations Ax = 0
- 5. The solution of non-homogeneous system of linear equations represented by Ax = b, existence of a solution when rank(A) = rank(A|b). The general solution of the system is the sum of a particular solution of the system and the solution of the associated homogeneous system.

Unit II: Determinants (15 Lectures)

Definition of determinant as an n-linear skew-symmetric function from $\mathbb{R}^n \times \mathbb{R}^n \times \cdots \times \mathbb{R}^n \to \mathbb{R}$ such that determinant of (E^1, E^2, \dots, E^n) is 1, where E^j denote the j^{th} column of the $n \times n$ identity matrix I_n .



- 2. Existence and uniqueness of determinant function via permutations, Computation of determinant of 2×2 , 3×3 matrices, diagonal matrices, basic results on determinants such as $\det(A^t) = \det(A)$, $\det(AB) = \det(A) \det(B)$, Laplace expansion of a determinant, Vandermonde determinant, determinant of upper triangular matrices and lower triangular matrices.
- 3. Linear dependence and independence of vectors in \mathbb{R}^n using determinants, the existence and uniqueness of the system Ax = b, where A is $n \times n$ matrix A, with $\det(A) \neq 0$, cofactors and minors, adjoint of an $n \times n$ matrix A, basic results such as A.Adj $(A) = \det(A)I_n$ An $n \times n$ real matrix A is invertible if and only if $\det(A) \neq 0$, $A^{-1} = \frac{1}{\det(A)} \operatorname{Adj}(A)$ for an invertible matrix A, Cramer's rule.

Unit III: Inner Product Spaces (15 Lectures)

- 1. Dot product in \mathbb{R}^n , Definition of an inner product on a vector space over \mathbb{R} , examples of inner product
- 2. Norm of a vector Cauchy-Schwarz inequality, triangle inequality, orthogonality of vectors, PythagoRUS theorem and geometric applications in \mathbb{R}^2 , Projections on a line, the projection being the closest approximation, Orthogonal complements of a subspace, orthogonal complements in \mathbb{R}^2 and \mathbb{R}^3 , orthogonal sets and orthonormal sets in an inner product space, orthogonal and orthonormal bases, Gram-Schmidt orthogonalization process, simple examples in \mathbb{R}^3 , \mathbb{R}^4 .

	Tutorials Based on Course : RUSMAT302					
Sr. No.	Tutorials					
1	Rank Numllity Theorem					
2	System of linear equations					
3	Determinants, calculating determinants of 2×2 , 3×3 matrices, $n \times n$ diagonal,					
3	upper triangular matrices using Laplace expansion.					
4	Finding inverses of 3×3 matrices using adjoint. Verifying $A.AdjA = (DetA)I_3$					
5	Examples of inner product spaces and orthogonal complements in \mathbb{R}^2 and \mathbb{R}^3 .					
6 7	Gram-Schmidt method					

Reference Books:



- (1) S. Lang, Introduction to Linear Algebra, Springer Verlag, 1997
- (2) S. Kumarasen, Linear Algebra A geometric approach, Prentice Hall of India Private Ltd, 2000
- (3) M. Artin, Algebra, Prentice Hall of India Private Ltd. 1991
- (4) K. HOFFMAN, R.KUNZE, Linear algebra, Tata McGraw-Hill, New Delhi. 1971
- (5) G. Strang, Linear Algebra and its applications, International student Edition. 2016
- (6) L. Smith, Linear Algebra and Springer Verlag. 1978
- (7) A. R. RAO AND P.BHIMASANKARAN, Linear Algebra, Tata McGraw-Hill, New Delhi. 2000
- (8) T. BANCHOFF, J. WERMER, Linear Algebra through Geometry. Springer Verlag New York, 1984.
- (9) S. AXLER, Linear Algebra done right, Springer Verlag, New York, 2015
- (10) K. Janich, Linear Algebra, Springer, 1994
- (11) O. Bretcher, Linear Algebra with Applications, Prentice Hall, 1996
- (12) G. Williams, Linear Algebra with Applications, Narosa Publication, 1984
- (13) H. Anton, Elementary Linear Algebra, Wiley, 2014.





Course Code: RUSMAT303 Course Title: Discrete Mathematics Academic Year: 2023-24

CO	CO Description	
CO1	to examine if given sets are countable.	
CO2	to experiment with addition and multiplication principle.	75
CO3	to solve recurrence relations.	
CO4	to extend notions of counting to multisets.	

Unit I: Preliminary Counting (15 Lectures)

- 1. Finite and infinite sets, countable and uncountable sets, examples such as \mathbb{N} , \mathbb{Z} , $\mathbb{N} \times \mathbb{N}$, \mathbb{Q} , (0,1), \mathbb{R}
- 2. Addition and multiplication principle, counting sets of pairs, two way counting, Permutation and Combination of sets.
- 3. Pigeonhole principle and its applications.

Unit II: Permutations and Recurrence relation (15 Lectures)

- 1. Permutation of objects, S_n composition of permutations, results such as every permutation is product of disjoint cycles, every cycle is product of transpositions, even and odd permutations, rank and signature of permutation, cardinality S_n , A_n .
- 2. Recurrence relation, definition of homogeneous, non-homogeneous, linear and non linear recurrence relation, obtaining recurrence relation in counting problems, solving (homogeneous as well as non homogeneous) recurrence relation by using iterative method, solving a homogeneous relation of second degree using algebraic method proving the necessary result.

Unit III: Advanced Counting (15 Lectures)

1. Binomial and Multinomial Theorem, Pascal identity, examples of standard identities such as the following



$$\bullet \sum_{k=0}^{r} \binom{m}{k} \binom{n}{r-k} = \binom{m+n}{r}$$

$$\bullet \sum_{i=r}^{n} \binom{i}{r} = \binom{n+1}{r+1}$$

$$\bullet \sum_{i=0}^{k} \binom{k}{i}^2 = \binom{2k}{k}$$

$$\bullet \sum_{i=0}^{n} \binom{n}{i} = 2^n$$

- 2. Permutations and combinations of multi-sets, circular permutations, emphasis on solving problems.
- 3. Non-negative and positive integral solutions of the equation $x_1 + x_2 + \cdots + x_r = n$.
- 4. Principle of Inclusion and Exclusion, its applications, derangements, explicit formulae for d_n , various identities involving d_n , deriving formula for Euler's phi function $\phi(n)$

	7 /								
	Practicals Based on Course : RUSMAT303								
Sr. No. Practicals									
1	Problems based on counting principles, two way counting.								
2	Pigeonhole principle.								
Signature of a permutation. Expressing permutation as the product of dicycles. Inverse of a permutation									
4	Recurrence relation.								
5	5 Multinomial theorem, identities, permutations and combinations of multi-sets.								
6 Inclusion-Exclusion principle, Derangements, Euler's phi function.									

Reference Books:

- (1) N. BIGGS, Discrete Mathematics, Oxford University Press, 1985
- (2) R. BRUShpi, Introductory Combinatorics, Pearson, 2010.
- (3) V. KRISHNAMURTHY, Combinatorics-Theory and Applications, Affiliated East West Press, 1985
- (4) A. Tucker, Applied Combinatorics, John Wiley and Sons, 1980
- $(5)\,$ S. S. Sane, Combinatorial Techniques, Hindustan Book Agency, 2013.



Modalities of Assessment

Theory Examination Pattern

(A) Internal Assessment - 40% 40 Marks

Sr. No.	Evaluation Type	Marks
1	Test	20
2	Assignment/Viva/Test/Presentation	20
	Total: 40 Marks	

(B) External Examination- 60% 60 Marks

- 1. Duration: These examinations shall be of **two hours duration**.
- 2. Theory Question Pattern

		Paper Pattern	,		
Question	Sub-question	Option	Marks	Questions Based on	
Question 1	a	Attempt any one of the given two questions.	20	Unit-I	
-	b	Attempt any two of the given four questions.			
Question 2	a	Attempt any one of the given two questions.	20	Unit-II	
-	b	Attempt any two of the given four questions.			
Question 3	a	Attempt any one of the given two questions.	20	Unit-III	
	b	Attempt any two of the given four questions.			
		Total Marks: 60			

Overall Examination and Marks Distribution Pattern Semester-III

Course RUSMAT301			RUSMAT302			RUSMAT303			Grand To-	
7	Internal External Total			Internal External Total			Practical	tal		
Theory	40	60	100	40	60	100	40	60	100	300



SEMESTER IV

Course Code: RUSMAT401 Course Title: Calculus of Several Variables Academic Year: 2023-24

CO	CO Description
CO1	to compare properties of functions of several variables with those of functions of one variable.
CO2	to deduce geometrical properties of surfaces and lines.
CO3	to apply the concept of differentiability to other sciences

Unit I: Functions of several variables (15 Lectures)

- 1. Euclidean space, \mathbb{R}^n norm, inner product, distance between two points, open ball in \mathbb{R}^n , definition of an open set / neighbourhood, sequences in \mathbb{R}^n , convergence of sequences (these concepts should be specifically discussed for $n \geq 2$ and n = 3).
- 2. Functions from $\mathbb{R}^n \to \mathbb{R}$ (scalar fields) and from $\mathbb{R}^n \to \mathbb{R}^n$ (Vector fields), sketching of regions in \mathbb{R}^2 and \mathbb{R}^3 . Graph of a function, level sets, cartesian coordinates, polar coordinates, spherical coordinates, cylindrical coordinates and conversions from one coordinate system to other. Iterated limits, limits and continuity of functions, basic results on limits and continuity of sum, difference, scalar multiples of vector fields, continuity of components of vector fields.
- 3. Directional derivatives and partial derivatives of scalar fields.
- 4. Mean value theorem for derivatives of scalar fields.

Unit II: Differentiation (15 Lectures)

- 1 Differentiability of a scalar field at a point (in terms of linear transformation) and in an open set; total derivative, uniqueness of total derivative of a differentiable function at a point, basic results on continuity, differentiability, partial derivative and directional derivative.
- 2. Gradient of a scalar field, geometric properties of gradient, level sets and tangent planes.



- 3. Chain rule for scalar fields.
- 4. Higher order partial derivatives, mixed partial derivatives, sufficient condition for equality of mixed partial derivative.

Unit III: Applications (15 Lectures)

- 1. Second order Taylor's formula for scalar fields.
- 2. Differentiability of vector fields, definition of differentiability of a vector field at Jacobian and Hessian matrix, differentiability of a vector field at a point implies continuity, the chain rule for derivative of vector fields (statement only).
- 3. Mean value inequality.
- 4. Maxima, minima and saddle points.
- 5. Second derivative test for extrema of functions of two variables.6. Method of Lagrange multipliers.

Tutorials Based on Course: RUSMAT401		
Sr. No.	Tutorials	
1	Sequences in \mathbb{R}^2 and \mathbb{R}^3 , limits and continuity of scalar fields and vector fields, using	
1	definition and otherwise, iterated limits.	
2	Computing directional derivatives, partial derivatives and mean value theorem of	
2	scalar fields.	
3	Total derivative, gradient, level sets and tangent planes.	
4	Chain rule, higher order derivatives and mixed partial derivatives of scalar fields.	
5	Taylor's formula, differentiation of a vector field at a point, finding Jacobian and	
3	Hessian matrix, Mean value inequality.	
6	Finding maxima, minima and saddle points, second derivative test for extrema of	
U	functions of two variables and method of Lagrange multipliers.	

Reference Books:

(1) S. R. GHORPADE, B. V. LIMAYE, A Course in Multivariable Calculus and Analysis, Springer, 2010.



- (2) T. Apostol, Calculus, Vol. 2, John Wiley, 1969.
- (3) J. Stewart, Calculus, Brooke/Cole Publishing Co., 1994.

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Course Code: RUSMAT402 Course Title: Linear Algebra III Academic Year: 2023-24

CO	CO Description	
CO1	to explain quotient structures on vector spaces.	
CO2	to explain the concepts of orthogonalization.	3
CO3	to apply the concepts of eigenvalues and eigenvectors to geometry.	>10

Unit I: Quotient Spaces and Orthogonal Linear Transformations (15 Lectures)

- (1) Review of vector spaces over \mathbb{R} , subspaces and linear transformations
- (2) Quotient spaces, first isomorphism theorem of real vector spaces (fundamental theorem of homomorphism of vector spaces), dimension and basis of the quotient space V/W, where V is finite dimensional vector space and W is subspace of V.
- (3) Orthogonal transformations, isometries of a real finite dimensional inner product space, translations and reflections with respect to a hyperplane, orthogonal matrices over \mathbb{R} , equivalence of orthogonal transformations and isometries fixing origin on a finite dimensional inner product space, orthogonal transformation of \mathbb{R} , any orthogonal transformation in \mathbb{R} is a reflection or a rotation, characterization of isometries as composites of orthogonal transformations and translation.
- (4) Characteristic polynomial of an $n \times n$ real matrix, Cayley Hamilton theorem and its applications (Proof assuming the result: $A \operatorname{Adj}(A) = \det(A) I_n$ for an $n \times n$ matrix A over the polynomial ring $\mathbb{R}[t]$).

Unit II: Eigenvalues and eigen vectors (15 Lectures)

(1) Eigen values and eigen vectors of a linear transformation $T: V \to V$ where V is a finite dimensional real vector space and examples, Eigen values and Eigen vectors of $n \times n$ real



matrices, linear independence of eigenvectors corresponding to distinct eigenvalues of a linear transformation and a matrix.

- (2) The characteristic polynomial of a $n \times n$ real matrix and a linear transformation of a finite dimensional real vector space to itself, characteristic roots, similar matrices, relation with change of basis, invariance of the characteristic polynomial and eigen values of similar matrices, every $n \times n$ square matrix with real eigenvalues is similar to an upper triangular matrix.
- (3) Minimal Polynomial of a matrix, examples, diagonal matrix, similar matrix, invariant subspaces.

Unit III: Diagonalisation (15 Lectures)

- (1) Geometric multiplicity and algebraic multiplicity of eigen values of an $n \times n$ real matrix, equivalent statements about diagonalizable matrix and multiplicities of its eigenvalues, examples of non diagonalizable matrices,
- (2) Diagonalisation of a linear transformation $T: V \to V$ where V is a finite dimensional real vector space and examples.
- (3) Orthogonal diagonalisation and quadratic forms, diagonalisation of real symmetric matrices, examples, applications to real quadratic forms, rank and signature of a real quadratic form
- (4) Classification of conics in \mathbb{R}^2 and quadric surfaces in \mathbb{R}^3 , positive definite and semi definite matrices, characterization of positive definite matrices in terms of principal minors.

Tutorials Based on Course : RUSMAT402		
Sr. No.	Tutorials	
1	Quotient spaces, orthogonal transformations.	
2	Cayley Hamilton theorem and applications.	
3	Eigenvalues and eigenvectors of a linear transformation and a square matrix.	
4	Similar matrices, minimal polynomial.	
5 ?	Diagonalization of a matrix.	
6	Orthogonal diagonalization and quadratic forms.	

Reference Books:



- (1) S. Kumaresan, Linear Algebra: A Geometric Approach, Prentice Hall of India, 2000
- (2) R. RAO, P. BHIMASANKARAM, Linear Algebra, TRIM, Hindustan Book Agency, 2000.
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 Rainarain Ruia (3) T. BANCHOFF, J. WERMER, Linear Algebra through Geometry, Springer, 1992.

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Course Code: RUSMAT403 Course Title: Ordinary Differential Equations Academic Year: 2023-24

CO	CO Description	
CO1	to classify the ODE according to degree and order of ODE.	
CO2	to solve an ODE.	(
CO3	to apply the concepts of ODE to biological sciences and physics	OK

Unit I: First order First degree Differential equations (15 Dectures)

- (1) Definition of a differential equation, order, degree, ordinary differential equation, linear and non linear ODE.
- (2) Existence and Uniqueness Theorem for the solutions of a second order initial value problem (statement only), Lipschitz function, examples
- (3) Review of solution of homogeneous and non-homogeneous differential equations of first order and first degree, notion of partial derivative, exact equations, general solution of exact equations of first order and first degree, necessary and sufficient condition for Mdx+Ndy=0 to be exact, non-exact equations, rules for finding integrating factors (without proof) for non exact equations and examples
- (4) Linear and reducible to linear equations, applications of first order ordinary differential equations.

Unit II: Second order Linear Differential equations (15 Lectures)

- (1) Homogeneous and non-homogeneous second order linear differentiable equations, the space of solutions of the homogeneous equation as a vector space, wronskian and linear independence of the solutions, the general solution of homogeneous differential equation, the use of known solutions to find the general solution of homogeneous equations, the general solution of a non-homogeneous second order equation, complementary functions and particular integrals.
- (2) The homogeneous equation with constant coefficient, auxiliary equation, the general solution corresponding to real and distinct roots, real and equal roots and complex roots of the auxiliary equation.



(3) Non-homogeneous equations, the method of undetermined coefficients, the method of variation of parameters.

Unit III: Power Series solution of ordinary differential equations (15 Lectures)

- 1. A review of power series.
- 2. Power series solutions of first order ordinary differential equations.
- 3. Regular singular points of second order ordinary differential equations.
- 4. Frobenius series solution of second order ordinary differential equations with regular singular points.

	Practicals Based on Course : RUSMAT403				
Sr. No.	Practicals				
1	Application of existence and uniqueness theorem, solving exact and non exact equa-				
1	tions.				
2	Linear and reducible to linear equations, applications to orthogonal trajectories,				
2	pop-ulation growth, and finding the current at a given time.				
3	Finding general solution of homogeneous and non-homogeneous equations, use of				
3	known solutions to find the general solution of homogeneous equations.				
4	Solving equations using method of undetermined coefficients and method of variation				
4	of parameters.				
5	Power series solutions of first order ordinary differential equations.				
6	Frobenius series method for second order ordinary differential equatuions.				

Reference Books:

- (1) G. F. SIMMONS, Differential Equations with Applications and Historical Notes, McGraw Hill, 1972.
- 2) E. A. CODDINGTON, An Introduction to Ordinary Differential Equations. Prentice Hall, 1961.
- (3) W. E. Boyce, R. C. DiPrima, Elementary Differential Equations and Boundary Value Problems, Wiely, 2013.



- (4) D. A. Murray, Introductory Course in Differential Equations, Longmans, Green and Co., 1897.
- (5) A. R. Forsyth, A Treatise on Differential Equations, MacMillan and Co., 1956.

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Modalities of Assessment

Theory Examination Pattern

(A) Internal Assessment - 40% 40 Marks

Sr. No.	Evaluation Type	Marks	
1	Test	20	
2	Assignment/Viva/Test/Presentation	20	1
	Total: 40 Marks		

(B) External Examination- 60% 60 Marks

- 1. Duration: These examinations shall be of **two hours duration**.
- 2. Theory Question Pattern

	Paper Pattern					
Question	Sub-question	Option	Marks	Questions Based on		
Question 1	a	Attempt any one of the given two questions.	20	Unit-I		
Question 1	b	Attempt any two of the given four questions.				
Question 2	a	Attempt any one of the given two questions.	20	Unit-II		
, and the second	b	Attempt any two of the given four questions.				
Question 3	a	Attempt any one of the given two questions.	20	Unit-III		
•	b	Attempt any two of the given four questions.				
	Total Marks: 60					

Overall Examination and Marks Distribution Pattern Semester-IV

Course RUSMAT401			RUSMAT402			RUSMAT403			Grand	
		To-								
\										tal
	Internal	External	Total	Internal	External	Total	Practical	External	Total	
Theory	40	60	100	40	60	100	40	60	100	300



Course Code: RUSMAT501 Course Title: Integral Calculus Academic Year: 2023-24

СО	CO Description	١,
CO1	to apply concepts of multiple integrals in the field of physics.	
CO2	to apply concepts of line integrals in the field of physics.	
CO3	to apply concepts of surface integrals in the field of physics.	

Unit I: Multiple Integrals (15 Lectures)

Definition of double (respectively: triple) integral of a function bounded on a rectangle (respectively: box), Geometric interpretation as area and volume. Fubini's Theorem over rectangles and any closed bounded sets, Iterated Integrals. Basic properties of double and triple integrals proved using the Fubini's theorem such as; Integrability of the sums, scalar multiples, products, and (under suitable conditions) quotients of integrable functions, Formulae for the integrals of sums and scalar multiples of integrable functions, integrability of continuous functions. More generally, integrability of bounded functions having finite number of points of discontinuity, Domain additivity of the integral. Integrability and the integral over arbitrary bounded domains. Change of variables formula (Statement only), Polar, cylindrical and spherical coordinates and integration using these coordinates. Differentiation under the integral sign. Applications to finding the center of gravity and moments of inertia.

Unit II: Line Integrals (15 Lectures)

Review of Scalar and Vector fields on \mathbb{R}^n . Vector Differential Operators, Gradient Paths (parametrized curves) in \mathbb{R} (emphasis on \mathbb{R} and \mathbb{R}), Smooth and piecewise smooth paths, Closed paths, Equivalence and orientation preserving equivalence of paths. Definition of the line integral of a vector field over a piecewise smooth path, Basic properties of line integrals including linearity, path-additivity and behavior under a change of parameters, Examples.

Line integrals of the gradient vector field, Fundamental Theorem of Calculus for Line Integrals, Necessary and sufficient conditions for a vector field to be conservative, Green's Theorem (proof



in the case of rectangular domains). Applications to evaluation of line integrals.

Unit III: : Surface Integrals (15 Lectures)

Parameterized surfaces. Smoothly equivalent parameterizations, Area of such surfaces. Definition of surface integrals of scalar-valued functions as well as of vector fields defined on a surface. Curl and divergence of a vector field, Elementary identities involving gradient, curl and divergence. Stoke's Theorem (proof assuming the general form of Green's Theorem), Examples Gauss' Divergence Theorem (proof only in the case of cubical domains), Examples.

Pract	icals Based on Course: RUSMAT501. Course Code: RUSMATP501-A
Sr. No.	Tutorials
1	Evaluation of double and triple integrals.
2	Change of variables in double and triple integrals and applications.
3	Line integrals of scalar and vector fields
4	Green's theorem, conservative field and applications
5	Evaluation of surface integrals
6	Stoke's and Gauss divergence theorem
7	Miscellaneous theory questions.

Reference Books:

- (1) T APOSTOL, Mathematical Analysis, Second Ed., Narosa, New Delhi. 1947.
- (2) R. COURANT AND F. JOHN, Introduction to Calculus and Analysis, Vol.2, Springer Verlag, New York, 1989.
- (3) W. Fleming, Functions of Several Variables, Second Ed., Springer-Verlag, New York, 1977.
- (4) M. H. PROTTER AND C. B. MORREY, JR., CIntermediate Calculus, Second Ed., Springer-Verlag, New York, 1995.
- (5) G. B. Thomas and R. L. Finney, Calculus and Analytic Geometry, Ninth Ed. (ISE Reprint), Addison- Wesley, Reading Mass, 1998.
- (6) D. V. Widder, Advanced Calculus, Second Ed., Dover Pub., New York. 1989



- (7) R COURANT AND F. JOHN., Introduction to Calculus and Analysis, Vol I. Reprint of 1st Ed. Springer-Verlag, New York, 1999.
- (8) SUDHIR R. GHORPADE AND BALMOHAN LIMAYE, A course in Multivariable Calculus and Analysis, Springer International Edition.

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Course Code: RUSMAT502 Course Title: Algebra II Academic Year: 2023-24

CO	CO Description	
CO1	to apply concepts of multiple integrals in the field of physics.	
CO2	to apply concepts of line integrals in the field of physics.	5
CO3	to apply concepts of surface integrals in the field of physics.	. 100

Unit 1: Group Theory

- i. Groups, definition and properties, examples such as $\mathbb{Z}, \mathbb{Q}, \mathbb{R}, \mathbb{C}, GL_n(\mathbb{R}), SL_n(\mathbb{R}), O_n$ (= the group of $n \times n$ real orthogonal matrices), B_n (= the group of $n \times n$ nonsingular upper triangular matrices), S_n , \mathbb{Z}_n , U(n) the group of prime, residue classes modulo n under multiplication, Quarternion group, Dihedral group as group of symmetries of regular n-gon, abelian group, finite and infinite groups.
- ii. Subgroups, necessary and sufficient condition for a non-empty subset of a group to be a subgroup. Examples, cyclic subgroups, centre $\mathcal{Z}(G)$.
- iii. Order of an element. Subgroup generated by a subset of the group. Cyclic group. Examples of cyclic groups such as \mathbb{Z} and the group μ_n of the n-th roots of unity.
- iv. Cosets of a subgroup in a group, Lagrange's Theorem.
- v. Homomorphisms, isomorphisms, automorphisms, kernel and image of a homomorphism.

Unit 2: Normal Subgroups

- i. Normal subgroup of a group, centre of a group, Alternating group A_n , cycles, Quotient group.
- ii. First Isomorphism Theorem, Second Isomorphism Theorem, Third Isomorphism Theorem, Correspondence Theorem.
- iii. Permutation groups, cycle decomposition, Cayley's Theorem for finite groups..



- iv. External direct product of groups, order of an element in a direct product, criterion for external product of finite cyclic groups to be cyclic.
- v. Classification of groups of order ≤ 7

Unit 3: Direct Product of Groups

- i. Internal direct product of subgroups, H and K which are normal in G, such that $H \cap K = \{1\}$. If a group is internal direct product of two normal subgroups H and K and HK = G, it is isomorphic to the external direct product $H \times K$.
- ii. Structure Theorem of finite abelian groups (statement only) and applications.
- iii. Conjugacy classes in a group, class equation. A group of order p^2 is abelian.

Pract	Practicals Based on Course: RUSMAT502. Course Code: RUSMATP501-B					
Sr. No.	Tutorials					
1	Examples and properties of groups					
2	Group of symmetry of equilateral triangle, rectangle, square.					
3	Subgroups					
4	Cyclic groups, cyclic subgroups, finding generators of every subgroup of a cyclic group.					
5	Left and right cosets of a subgroup, Lagrange's Theorem.					
6	Group homomorphisms, isomorphisms.					
7	Miscellaneous Theory Questions					

Reference Books

- (1) I. N. Herstein, Topics in Algebra, Wiley Eastern Limited, Second edition.
- (2) Michael Artin, Algebra, Prentice Hall of India, New Delhi.
- (3) P.B. Bhattacharya, S. K. Jain and S. R. Nagpaul, Basic Abstract Algebra, Second edition, Foundation Books, New Delhi, 1995.



(4) D. Dummit, R. Foote, Abstract Algebra, John Wiley and Sons, Inc.

Additional Reference Books:

- (1) N. S. Gopalakrishnan, University Algebra, Wiley Eastern Limited.
- (2) J. Gallian, Contemporary Abstract Algebra, Narosa, New Delhi.

arosa, New Del College College



Course Code:RUSMAT503 Course Title: Topology of Metric Spaces Academic Year: 2023-24

CO	CO Description
CO1	to construct examples of metrics.
CO2	to compare properties of open, closed intervals, sequences and completeness on R
CO2	with an arbitrary metric space.
CO3	to compare properties of continuity on R with an arbitrary metric space.

Unit I: Metric Spaces (15 Lectures)

Definition, examples of metric spaces \mathbb{R} , \mathbb{R}^2 Euclidean space \mathbb{R}^n sup and sum metric, \mathbb{C} (complex numbers), normed spaces. distance metric induced by the norm, translation invariance of the metric induced by the norm. Metric subspaces. Product of two metric spaces. Open balls and open sets in a metric space, examples of open sets in various metric spaces, Hausdorff property, interior of a set. Structure of an open set in \mathbb{R} , equivalent metrics. Distance of a point from a set, distance between sets, diameter of a set in a metric space and bounded sets.

Unit II: Closed sets, Sequences, Completeness (15 Lectures)

Closed ball in a metric space, Closed sets-definition, examples. Limit point of a set, Isolated point, A closed set contains all its limit points, Closure of a set and boundary, Sequences in a metric space, Convergent sequence in a metric space, Cauchy sequence in a metric space, subsequences, examples of convergent and Cauchy sequence in finite metric spaces, \mathbb{R} with different metrics and other metric spaces. Characterization of limit points and closure points in terms of sequences. Definition and examples of relative openness/closeness in subspaces, Dense subsets in a metric space and Separability. Definition of complete metric spaces, Examples of complete metric spaces. Completeness property in subspaces. Nested Interval theorem in \mathbb{R} . Cantor's Intersection Theorem.

Unit III: Continuity (15 Lectures)

Epsilon-delta definition of continuity at a point of a function from one metric space to another. Equivalent characterizations of continuity at a point in terms of sequences, open sets and closed sets and examples. Algebra of continuous real valued functions on a metric space. Continuity of



the composite of continuous functions.

Pract	Practicals Based on Course : RUSMAT503. Course Code: RUSMATP502-A				
Sr. No.	Tutorials				
1	Examples of Metric Spaces.				
2	Open balls and Open sets in Metric / Normed Linear spaces, Interior Points.				
3	Subspaces, Closed Sets and Closure, Equivalent Metrics and Norms.				
4	Sequences, Convergent and Cauchy Sequences in a Metric Space, Complete Metric				
4	Spaces, Cantors Intersection Theorem and its Applications.				
5	Continuous Functions on Metric Spaces				
6	Characterization of continuity at a point in terms of metric spaces.				
7	Miscellaneous Theory Questions.				
1					

Reference Books:

- (1) S. Kumaresan, Topology of Metric spaces, Narosa, Second Edn.
- (2) E. T. COPSON., Metric Spaces. Universal Book Stall, New Delhi, 1996.

Additional Reference Books:

- (1) W. Rudin, Principles of Mathematical Analysis, Third Ed, McGraw-Hill, Auckland, 1976.
- (2) T. Apostol, Mathematical Analysis, Second edition, Narosa, New Delhi, 1974
- (3) P. K. Jain. K. Ahmed, Metric Spaces. Narosa, New Delhi, 1996.
- (4) R. R. GOLDBERG, Methods of Real Analysis, Oxford and IBH Pub. Co., New Delhi 1970.
- (5) D. Somasundaram, B. Choudhary, A first Course in Mathematical Analysis. Narosa, New Delhi
- (6) G.F. Simmons, Introduction to Topology and Modern Analysis, McGraw-Hii, New York, 1963.
- (7) SUTHERLAND, Introduction to Metric and Topological Spaces, Oxford University Press, 2009



Course Code: RUSMATE504I Course Title: Graph Theory Academic Year: 2023-24

СО	CO Description	
CO1	to understand various aspects of factorization	
CO2	to understand importance of cryptography in todays world.	4

Unit I: Basics of Graphs (15 Lectures)

Definition of general graph, Directed and undirected graph, Simple and multiple graph, Types of graphs- Complete graph, Null graph, Complementary graphs, Regular graphs Sub graph of a graph, Vertex and Edge induced sub graphs, Spanning sub graphs. Basic terminology- degree of a vertex, Minimum and maximum degree, Walk, Trail, Circuit, Path, Cycle. Handshaking theorem and its applications, Isomorphism between the graphs and consequences of isomorphism between the graphs, Self complementary graphs, Connected graphs, Connected components. Matrices associated with the graphs – Adjacency and Incidence matrix of a graph- properties, Bipartite graphs and characterization in terms of cycle lengths. Degree sequence and Havel-Hakimi theorem.

Unit II: Trees (15 Lectures)

Cut edges and cut vertices and relevant results, Characterization of cut edge, Definition of a tree and its characterizations, Spanning tree, Recurrence relation of spanning trees and Cayley formula for spanning trees, Prefix codes and Huffman coding, Weighted graphs.

Unit III: Eulerian and Hamiltonian graphs (15 Lectures)

Eulerian graph and its characterization, Hamiltonian graph, Necessary condition for Hamiltonian graphs using G-S where S is a proper subset of V(G), Sufficient condition for Hamiltonian graphs-Ore's theorem and Dirac's theorem, Hamiltonian closure of a graph, Cube graphs and properties like regular, bipartite, Connected and Hamiltonian nature of cube graph, Line graph of a graph and simple results.

3	
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Pract	Practicals Based on Course RUSMATE504I. Course Code: RUSMATP502-B					
Sr. No.	Tutorials					
1	Handshaking Lemma and Isomorphism.					
2	Degree Sequence					
3	Trees, Cayley Formula.					
4	Applications of Trees.					
5	Eulerian Graphs.					
6	Hamiltonian Graphs.					
7	Miscellaneous Problems.					

Reference Books:

- (1) BONDY AND MURTY, Graph Theory with Applications
- (2) Balkrishnan and Ranganathan, Graph theory and applications.
- (3) WEST D. B. , Introduction to Graph Theory, Pearson Modern Classics for Advanced Mathematics Series, 2^{nd} Edn.
- (4) Sharad Sane, Combinatorial Techniques, Hindustan Book Agency.

Additional Reference Books:

- (1) BEHZAD AND CHARTRAND, Graph theory
- (2) CHOUDAM S. A., Introductory Graph theory.





Course Code: RUSMATE504II Course Title: Number Theory and its Applications Academic Year: 2023-24

CO	CO Description	
CO1	to understand various aspects of factorization]
CO2	to understand importance of cryptography in todays world.	7

Unit 1: Congruences and Factorization

Congruences: Definition and elementary properties, Complete residue system modulo m, Reduced residue system modulo m, Euler's function and its properties, Fermat's Little Theorem, Euler's generation of Fermat's Little Theorem, Wilson's Theorem, Linear congruence, The Chinese Remainder Theorem, Congruence of higher degree, The Fermat-Kraitchik Factorization Method.

Unit 2: Diophantine Equations and their Solutions

The linear equations ax + by = c. The equations $x^2 + y^2 = p$ where p is a prime. The equation $x^2 + y^2 = z^2$, Pythagorean triples, primitive solutions, The equations $x^4 + y^4 = z^2$ and $x^4 + y^4 = z^4$ have no solutions (x, y, z) with $xyz \neq 0$. Every positive integer n can be expressed as sum of squares of four integers, Universal quadratic forms $x^2 + y^2 + z^2 + t^2$. Assorted examples –section 5.4 of Number theory by Niven-Zuckermann-Montgomery.

Unit 3: Primitive Roots and Cryptography

Order of an integer and Primitive Roots. Basic notions such as encryption (enciphering) and decryption (deciphering), Cryptosystems, symmetric key cryptography, Simple examples such as shift cipher, Affine cipher, Hill's cipher, Vigenere cipher. Concept of Public Key Cryptosystem; RSA Algorithm. An application of Primitive Roots to Cryptography.



Practi	Practicals Based on Course RUSMATE504II. Course Code: RUSMATP602-B					
Sr. No.	Tutorials					
1	Congruences.					
2	Linear congruences and congruences of higher degree.					
3	Linear diophantine equations.					
4	Pythagorean triples and sum of squares.					
5	Cryptosystems (Private Key).					
6	Cryptosystems (Public Key) and primitive roots.					
7	Miscellaneous theoretical questions.					

Reference Books:

- (1) David M. Burton, An Introduction to the Theory of Numbers. Tata McGraw Hill Edition.
- (2) Niven, H. Zuckerman and H. Montogomery, An Introduction to the Theory of Numbers, John Wiley and Sons. Inc.
- (3) M. Artin, Algebra. Prentice Hall.
- (4) K. Ireland, M. Rosen. A classical introduction to Modern Number Theory. Second edition, Springer Verlag.





Modalities of Assessment

Theory Examination Pattern

(A) Internal Assessment - 40% 40 Marks

Sr. No.	Evaluation Type	Marks
1	Test	20
2	Assignment/Viva/Test/Presentation	20
	Total: 40 Marks	

(B) External Examination- 60% 60 Marks

- Duration: These examinations shall be of two hours duration.
 Theory Question Pattern

		Paper Pattern			
Question	Sub-question	Option	Marks	Questions Based or	
Question 1	a	Attempt any one of the given two questions.	20	Unit-I	
Q	b	Attempt any two of the given four questions.		0	
Question 2	a	Attempt any one of the given two questions.	20	Unit-II	
•	b	Attempt any two of the given four questions.			
Question 3	a	Attempt env one of the given two questions.	20	Unit-III	
	b	Attempt any two of the given four questions. Total Marks: 60			
	Maj.				



Practical Examination Pattern

(A) Internal Assessment - 40% 20 Marks

Sr. No.	Evaluation Type	Marks			
1	1 Journal				
2	2 Viva/ Multiple Choice Questions				
	Total: 20 Marks	4			

(B) External Examination- 60% 60 Marks

- 1. Duration: These examinations shall be of **two hours duration**.
- 2. Theory Question Pattern

External Examination- 60% 30 Marks

Paper Pattern	
There shall be three compulsory questions of 10 marks each with internal choice	30 Msrks
Total Marks: 30	

Overall Examination and Marks Distribution Pattern Semester-V

Course	RUSMAT501			RUSMAT502		RUSMAT503			RUSMAT504			Grand	
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	• /		• •								tal		
	Internal	External	Total	Internal	External	Total	Internal	External	Total	Internal	External	Total	
Theory	40	60	100	40	60	100	40	60	100	40	60	100	400
Practicals	20	30	50	20	30	50	20	30	50	20	30	50	200



Course Code: RUSMAT601 Course Title: Basic Complex Analysis Academic Year: 2023-24

CO	CO Description	
CO1	to elaborate on properties of complex numbers.]
CO2	to elaborate on properties of Mobius transforms and singularities in subsets of C.	4

Unit I: Complex Numbers and Functions of Complex variables (15 Lectures)

Review of complex numbers: Complex plane, polar coordinates, exponential map, powers and roots of complex numbers, De Moivr's formula, \mathbb{C} as a metric space, bounded and unbounded sets, point at infinity-extended complex plane, sketching of set in complex plane.

Limit at a point, theorems on limits, convergence of sequences of complex numbers and results using properties of real sequences. Functions $f: \mathbb{C} \to \mathbb{C}$ real and imaginary part of functions, continuity at a point and algebra of continuous functions.

Unit II: Holomorphic functions (15 Lectures)

Derivative of $f: \mathbb{C} \to \mathbb{C}$; comparison between differentiability in real and complex sense, Cauchy-Riemann equations, sufficient conditions for differentiability, analytic function, ', f, g analytic then f+g, f-g, fg, f/g are analytic, chain rule. Theorem: If f'=0 everywhere in a domain G then f must be constant throughout, Harmonic functions and harmonic conjugate.

Explain how to evaluate the line integral $\int f(z)dz$ over $|z-z_0|=r$ and prove the Cauchy integral formula: If f is analytic in $B(z_0,r)$ then for any w in $B(z_0,r)$ we have $f(w)=\int \frac{f(z)}{w-z}dz$ over $|z-z_0|=r$.

Unit III: Complex power series (15 Lectures)

Taylor's theorem for analytic functions, Mobius transformations—definition and examples. Exponential function, its properties, trigonometric function, hyperbolic functions, Power series of complex numbers and related results, radius of convergences, disc of convergence, uniqueness of series representation, examples.



Definition of Laurent series, Definition of isolated singularity, statement (without proof) of existence of Laurent series expansion in neighbourhood of an isolated singularity, type of isolated singularities viz. removable, pole and essential defined using Laurent series expansion, statement of residue theorem and calculation of residue.

Prac	Practicals Based on Course RUSMAT601. Course Code:RUSMATP601-A				
Sr. No.	Practicals				
1	Complex Numbers, subsets of $\mathbb C$ and their properties.				
2	Limits and continuity of complex-valued functions .				
3	Derivatives of functions of complex variables, analytic functions.				
4	Analytic function, finding harmonic conjugate, Mobius transformations.				
5	Cauchy integral formula, Taylor series, power series.				
6	Finding isolated singularities- removable, pole and essential, Laurent series, Calcu-				
0	lation of residue.				
7	Miscellaneous theory questions.				

Reference Books:

Reference Books:

- (1) J. W. Brown and R.V. Churchill, Complex analysis and Applications.
- (2) S. Ponnusamy, Foundations Of Complex Analysis, Second Ed., Narosa, New Delhi. 1947
- (3) R. E. GREENE AND S. C. KRANTZ, Function theory of one complex variable
- (4) T. W. GAMELIN, Complex analysis



Course Code: RUSMAT602 Course Title: Algebra III Academic Year: 2023-24

CO	CO Description
CO1	to extend concept of normal subgroup to ideal of the ring R.
CO2	to elaborate properties of ED, PID and UFD.
CO3	to find quadratic extensions of field F.

Unit 1: Ring Theory

- i. Ring (definition should include the existence of a unity element), zero divisor, unit, the multiplicative group of units of a ring. Basic properties and examples of rings.
- ii. Commutative ring, integral domain, division ring, subring, examples, Characteristic of a ring, characteristic of an Integral Domain.
- iii. Ring homomorphism, kernel of ring homomorphism, ideals, operations on ideals and quotient rings, examples.
- iv. Factor theorem and First and Second isomorphism theorems for rings, Correspondence theorem for rings.

Unit 2: Factorization

- i. Principal ideal, maximal ideal, prime ideal, characterization of prime and maximal ideals in terms of quotient rings.
- ii. Polynomial rings, R[X] when R is an integral domain/ field, Eisenstein's criterion for irreducibility of a polynomial over \mathbb{Z} , Gauss lemma, prime and maximal ideals in polynomial rings.
- iii Notions of euclidean domain (ED), principal ideal domain (PID) and unique factorization domain (UFD). Relation between these three notions (ED \Rightarrow PID \Rightarrow UFD).
- iv Example of ring of Gaussian integers.

Unit 3: Field Theory

i. Review of field, characteristic of a field, Characteristic of a finite field is prime.



- ii. Prime subfield of a field, Prime subfield of any field is either \mathbb{Q} or \mathbb{Z}_p (upto isomorphism).
- iii. Field extension, Degree of field extension. Algebraic elements, Any homomorphism of a field is injective.
- iv. Any irreducible polynomial p(x) over a field F has a root in an extension of the field, moreover the degree of this extension $\frac{F(x)}{(p(x))}$ over the field F is the degree of the polynomial p(x).
- v. The extension $\frac{\mathbb{Q}[x]}{(x^2-2)}$ i.e. $\mathbb{Q}(\sqrt{2})$, $\frac{\mathbb{Q}[x]}{(x^3-2)}$ i.e. $\mathbb{Q}(\sqrt[3]{2})$, $\frac{\mathbb{Q}[x]}{(x^2+1)}$ i.e. $\mathbb{Q}(i)$, Quadratic extensions of a field F when characteristic of F is not 2.

Prac	Practicals Based on Course RUSMAT602. Course Code: RUSMATP601-B							
Sr. No.	Tutorials							
1	Rings, Subrings							
2	Ideals, Ring Homomorphism and Isomorphism							
3	Polynomial Rings							
4	Prime and Maximal Ideals							
5	Fields, Subfields							
6	Field Extensions							
7	Miscellaneous Theory Questions							

Reference Books:

- (1) I. N. Herstein, Topics in Algebra, Wiley Eastern Limited, Second edition.
- (2) Michael Artin, Algebra, Prentice Hall of India, New Delhi.
- (3) P.B. Bhattacharva, S. K. Jain and S. R. Nagpaul, Basic Abstract Algebra, Second edition, Foundation Books, New Delhi, 1995.
- (4) D. Dummit, R. Foote, Abstract Algebra, John Wiley and Sons, Inc.

Additional Reference Books:

- (1) N. S. Gopalakrishnan, University Algebra, Wiley Eastern Limited.
- (2) J. Gallian, Contemporary Abstract Algebra, Narosa, New Delhi.



- (3) J. B. Fraleigh, A First Course in Abstract Algebra, Third edition, Narosa, New Delhi.
- (4) T. W. Hungerford, Algebra, Springer.

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Rannanain Ruia



Course Code: RUSMAT603 Course Title: Metric Topology Academic Year: 2023-24

CO	CO Description
CO1	to compare properties of compact and connected sets on R with an arbitrary metric spaces.
CO2	to elaborate on properties of sequences and series of functions.

Unit I: Compact Sets (15 Lectures)

Definition of compact metric space using open cover, examples of compact sets in different metric spaces \mathbb{R} , \mathbb{R}^2 , \mathbb{R}^3 and other metric spaces. Properties of compact sets:compact set is closed and bounded, every infinite bounded subset of a compact metric space has a limit point, Heine Borel theorem-every subset of Euclidean metric space \mathbb{R} is compact if and only if it is closed and bounded. Equivalent statements for compact sets in \mathbb{R} ; Heine-Borel property, Closed and boundedness property, Bolzano-Weierstrass property, Sequentially compactness property. Finite intersection property of closed sets for compact metric space, hence every compact metric space is complete.

Unit II: Connected sets (15 Lectures)

Separated sets- definition and examples, disconnected sets, disconnected and connected metric spaces, Connected subsets of a metric space. Connected subsets of \mathbb{R} , A subset of \mathbb{R} is connected if and only if it is an interval. A continuous image of a connected set is connected, Characterization of a connected space, viz. a metric space is connected if and only if every continuous function from b to <1,-1> is a constant function. Path connectedness in \mathbb{R} , definition and examples, A path connected subset of \mathbb{R} is connected, convex sets are path connected, Connected components, An example of a connected subset of \mathbb{R} which is not path connected.

Unit III: Sequence and series of functions (15 Lectures)

Sequence of functions - pointwise and uniform convergence of sequences of real-valued functions, examples. Uniform convergence implies pointwise convergence, example to show converse



not true, series of functions, convergence of series of functions, Weierstrass M-test. Examples. Properties of uniform convergence: Continuity of the uniform limit of a sequence of continuous function, conditions under which integral and the derivative of sequence of functions converge to the integral and derivative of uniform limit on a closed and bounded interval. Examples. Consequences of these properties for series of functions, term by term differentiation and integration. Power series in $\mathbb R$ centered at origin and at some point 4F in $\mathbb R$, radius of convergence, region (interval) of convergence, uniform convergence, term by-term differentiation and integration of power series, Examples. Uniqueness of series representation, functions represented by power series, classical functions defined by power series such as exponential, cosine and sine functions, the basic properties of these functions.

Prac	Practicals Based on Course RUSMAT603. Course Code: RUSMATP602-A							
Sr. No.	Practicals							
1	Examples of compact metric spaces.							
2	Equivalent conditions for a subset of a metric space to be compact							
3	Connectedness							
4	Path Connectedness							
5	Pointwise and uniform convergence of sequence of functions.							
6	Pointwise and uniform convergence of series of functions and power series							
7	Miscellaneous Theory Questions.							

Reference Books:

- (1) S. Kumaresan, Topology of Metric spaces. Narosa, Second Edn.
- (2) E. T. COPSON., Metric Spaces. Universal Book Stall, New Delhi, 1996.
- (3) R. R. GOLDBERG, Methods of Real Analysis, Oxford and IBH Pub. Co., New Delhi 1970.

Additional Reference Books:

- (1) W. Rudin, Principles of Mathematical Analysis, Third Ed, McGraw-Hill, Auckland, 1976.
- (2) T. Apostol, Mathematical Analysis, Second edition, Narosa, New Delhi, 1974
- (3) E. T. COPSON., Metric Spaces. Universal Book Stall, New Delhi, 1996.
- (4) P. K. Jain. K. Ahmed, Metric Spaces. Narosa, New Delhi, 1996.



- (5) D. Somasundaram, B. Choudhary, A first Course in Mathematical Analysis. Narosa, New Delhi
- (6) G.F. Simmons, Introduction to Topology and Modern Analysis, McGraw-Hii, New York, 1963.

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Course Code: RUSMATE604I Course Title: Graph Theory and Combinatorics Academic Year: 2023-24

CO	CO Description
CO1	to apply the concepts of colorings of graphs and planar graph in the fields of chem-
	istry, physics and biological sciences.
CO2	to apply the concepts of combinatorics in the field of statistics.

Unit I: Colorings of graphs (15 Lectures)

Vertex coloring- evaluation of vertex chromatic number of some standard graphs, critical graph. Upper and lower bounds of Vertex chromatic Number- Statement of Brooks theorem. Edge coloring- Evaluation of edge chromatic number of standard graphs such as complete graph, complete bipartite graph, cycle. Statement of Vizing Theorem. Chromatic polynomial of graphs-Recurrence Relation and properties of Chromatic polynomials. Vertex and Edge cuts vertex and edge connectivity and the relation between vertex and edge connectivity. Equality of vertex and edge connectivity of cubic graphs. Whitney's theorem on 2-vertex connected graphs.

Unit II: Planar graphs (15 Lectures)

Definition of planar graph. Euler formula and its consequences. Non planarity of K_5 ; K(3;3). Dual of a graph. Polyhedran in \mathbb{R} and existence of exactly five regular polyhedra- (Platonic solids) Colorabilty of planar graphs- 5 color theorem for planar graphs, statement of 4 color theorem.

Unit III: Combinatorics (15 Lectures)

Applications of Inclusion Exclusion Principle- Rook polynomial, Forbidden position problems Introduction to partial fractions and using Newton's binomial theorem for real power series, expansion of some standard functions. Forming recurrence relation and getting a generating function. Solving a recurrence relation using ordinary generating functions. System of Distinct



Representatives and Hall's theorem of SDR.

Practi	Practicals Based on Course RUSMATE604II. Course Code: RUSMATP602-B								
Sr. No.	Tutorials								
1	Coloring of Graphs.								
2	Chromatic polynomial and connectivity								
3	Planar graphs.								
4	Inclusion Exclusion Principle and Recurrence relation.								
5	Rook polynomial.								
6	Generating Functions and System of Distinct Representatives.								
7	Miscellaneous Problems.								

Reference Books:

- (1) BONDY AND MURTY, Graph Theory with Applications
- (2) Balkrishnan and Ranganathan, Graph theory and applications.
- (3) WEST D B, Introduction to Graph Theory, Pearson Modern Classics for Advanced Mathematics Series, 2^{nd} Edn
- (4) RICHARD BRUSLDI, Introduction to Combinatorics.
- (5) Sharad Sane, Combinatorial Techniques, Hindustan Book Agency.

Additional Reference Books:

- (1) Behzad and Chartrand , Graph theory, Pearson Modern Classics for Advanced Mathematics Series, 2^{nd} Edn.
- (2) CHOUDAM S. A., Introductory Graph theory.
- (3) Cohen, Combinatorics



Course Code: RUSMATE604II Course Title: Number Theory and its Applications Academic Year: 2023-24

CO	CO Description	
CO1	to apply Gauss Lemma in different situations.	
CO2	to understand continuied fractions.	(
CO3	to understand and apply theory of arithmetic functions in simple situations.	7

Unit 1: Quadratic Reciprocity

Quadratic Residues and Legendre Symbol, Euler's criterion, Gauss's Lemma, Quadratic Reciprocity Law. The Jacobi Symbol and law of reciprocity for Jacobi Symbol. Quadratic Congruences with Composite moduli.

Unit 2: Continued Fractions

Finite continued fractions. Infinite continued fractions and representation of an irrational number by an infinite simple continued fraction, Rational approximations to irrational numbers and order of convergence, Best possible approximations. Periodic continued fractions.

Unit 3: Pell's Equation, Arithmetic Functions and Special Numbers

Pell's equation $x^2 - dy^2 = n$, where d is not a square of an integer. Solutions of Pell's equation (The proofs of convergence theorems to be omitted). Arithmetic functions of number theory: d(n) (or T(n)), $\sigma(n)$, $\sigma(n)$, w(n) and their properties, $\mu(n)$ and the Mobius inversion formula. Special numbers: Fermat numbers, Mersenne numbers, Perfect numbers, Amicable numbers, Pseudo primes, Carmichael numbers.

Prac	Practicals Based on Course RUSMATE604II. Course Code: RUSMATP602							
Sr. No.	Tutorials							
1	Legendre Symbol.							
2	Jacobi Symbol and Quadratic congruences with composite moduli.							
3	Finite continued fractions.							
4	Infinite continued fractions.							
5	Pell's equations and Arithmetic functions of number theory.							
6	Special Numbers.							
7	Miscellaneous theoretical questions.							



Reference Books:

- (1) David M. Burton, An Introduction to the Theory of Numbers. Tata McGraw Hill Edition.
- (2) Niven, H. Zuckerman and H. Montogomery, An Introduction to the Theory of Numbers, John Wiley and Sons. Inc.
- (3) M. Artin, Algebra. Prentice Hall.
- (4) K. Ireland, M. Rosen. A classical introduction to Modern Number Theory. Second edition



Modalities of Assessment

Theory Examination Pattern

(A) Internal Assessment - 40% 40 Marks

Sr. No.	Evaluation Type	Marks
1	Test	20
2	Assignment/Viva/Test/Presentation	20)
	Total: 40 Marks	

(B) External Examination- 60% 60 Marks

		Paper Pattern			
Question	Sub-question	Option	Marks	Questions Based on	
Question 1	a	Attempt any one of the given two questions.	20	Unit-I	
Question 1	b	Attempt any two of the given four questions.			
Question 2	a	Attempt any one of the given two questions.	20	Unit-II	
Question 2	b	Attempt any two of the given four questions.	20		
Question 3	a	Attempt any one of the given two questions.	20	Unit-III	
Question 5	b	Attempt any two of the given four questions.	20	01110-111	
	•	Total Marks: 60			



Practical Examination Pattern

(A) Internal Assessment - 40% 20 Marks

Sr. No.	Evaluation Type							
1	Journal	5						
2	2 Viva/ Multiple Choice Questions							
	Total: 20 Marks							

(B) External Examination- 60% 60 Marks

- 1. Duration: These examinations shall be of **two hours duration**.
- 2. Theory Question Pattern

External Examination- 60% 30 Marks

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Paper Pattern
There shall be three compulsory questions of 10 marks each with internal choice 30 Msrks
Total Marks: 30

Overall Examination and Marks Distribution Pattern Semester-VI

Course	RUSMAT601			RU	SMAT60	2	RUSMAT603		RUSMAT604			Grand	
				,									То-
	• •												tal
	Internal	External	Total	Internal	External	Total	Internal	External	Total	Internal	External	Total	
Theory	40	60	100	40	60	100	40	60	100	40	60	100	400
Practicals	20	30	50	20	30	50	20	30	50	20	30	50	200